Minitest 4 - MTH 1410 Dr. Adam Graham-Squire, Fall 2017

Name: _____

I pledge that I have neither given nor received any unauthorized assistance on this exam.

(signature)

DIRECTIONS

- 1. Don't panic.
- 2. <u>Show all of your work and use correct notation</u>. A correct answer with insufficient work or incorrect notation will lose points.
- 3. Clearly indicate your answer by putting a box around it.
- 4. Cell phones and computers are <u>not</u> allowed on this test. Calculators <u>are</u> allowed on the first 5 questions of the test, however you should still show all of your work. No calculators are allowed on the last question of the test.
- 5. Give all answers in exact form, not decimal form (that is, put π instead of 3.1415, $\sqrt{2}$ instead of 1.414, etc) unless otherwise stated.
- 6. Make sure you sign the pledge above.
- 7. Number of questions = 5. Total Points = 30.

1. (5 points) Calculate the definite integral. Show your work and give an <u>exact</u> answer (No decimal approximation, though if you want to use your calculator to confirm that your answer is correct, a decimal approximation may be useful).

$$\int_{1}^{4} \left(\frac{e^x}{3} - \frac{7}{x^3}\right) dx$$

2. (5 points) Let $g(x) = \int_3^x t^2(t-4)(t+2)dt$, where g is defined for all values of x. On what interval(s) is g(x) increasing? You should not need a calculator to solve this problem, but you can use one if you think it will help you.

No Calculator

Name:_____

3. (5 points) Calculate the indefinite integral:

$$\int \left(\frac{x^2}{x^3} + \frac{3}{1+x^2} - (\csc x)(\cot x)\right) dx$$

4. (6 points) Calculate the indefinite integral:

$$\int x^3 (3-2x^4)^3 \, dx$$

5. (9 points) Below, the first few steps are done for using the limit definition to calculate a definite integral. Answer the questions below (a brief answer is sufficient). You can use the blank next page if you need more room.

$$\int_0^3 x^2 dx = \lim_{n \to \infty} \sum_{i=1}^n f(x_i) \Delta x \tag{1}$$

$$= \lim_{n \to \infty} \frac{3}{n} \left[f\left(\frac{3}{n}\right) + f\left(\frac{6}{n}\right) + f\left(\frac{9}{n}\right) + \dots + f\left(\frac{3n}{n}\right) \right]$$
(2)

$$= \lim_{n \to \infty} \frac{3}{n} \left[\left(\frac{3}{n} \right)^2 + \left(\frac{6}{n} \right)^2 + \left(\frac{9}{n} \right)^2 + \dots + \left(\frac{3n}{n} \right)^2 \right]$$
(3)

$$= \lim_{n \to \infty} \frac{3}{n} \left(\frac{3}{n} \right)^2 \left[1^2 + 2^2 + 3^2 + \dots + n^2 \right]$$
(4)

- (a) Explain where the $\frac{3}{n}$ comes from (between lines 1 and 2).
- (b) Explain why all of the terms are squared in line 3.
- (c) Explain what is happening between lines 3 and 4.
- (d) Use the magic formula $1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$ to help you finish off calculating the limit.
- (e) Use the Fundamental Theorem of Calculus (the evaluation theorem) to calculate $\int_0^3 x^2 dx$ to double-check your answer from (d).

Extra Credit(1 point) If $\int_0^{10} f(x) dx = 42$, $\int_0^3 f(x) dx = -7$, $\int_7^3 f(x) dx = -12$, and $\int_9^{10} 3f(x) dx = 60$, what is $\int_7^9 f(x) dx$?